

**MATH1003**  
**QUIZ 2**

*This quiz has four questions, with each question worth 5 marks.*

*The quiz lasts for thirty minutes. No calculator, textbooks, or other notes are allowed.*

1. Let:

$$f(x) = \begin{cases} \frac{x^2 - 4}{x - 2}, & \text{when } x < 2; \\ ax^2 - bx + 3, & \text{when } 2 \leq x < 3; \\ 2x - a + b, & \text{when } x \geq 3. \end{cases}$$

Find the values of  $a$  and  $b$  that make  $f$  continuous everywhere.

2. Use the Intermediate Value Theorem to show that there is a solution to each of the following equations in the specified intervals:

(i)  $\cos x = x$  in the interval  $(0, 1)$ ,

(ii)  $\ln x = e^{-x}$  in the interval  $(1, 2)$ .

3. Find the horizontal and vertical asymptotes of  $y = \frac{x^2 + 1}{2x^2 - 3x - 2}$ . Use this information to sketch the graph.

4. Find the derivative of  $y = \tan^2 3x$ .